# Design and Simulation of PSO Based PI Controller for a Non-Linear Two-Tank Interacting Level Process

### R.Soundariya, Dr.S.Arulselvi

*Abstract*— In this work, a non linear two-tank interacting level process is taken-up for study. The mathematical model of the two-tank interacting process is derived. A conventional PI controller is designed based on process reaction curve with ZN technique. To improve the performance of PI controller, a Particle Swarm Optimization (PSO) based PI controller PSO-PI is proposed and implemented. The servo and regulatory responses with PI and PSO-PI are obtained and discussed. From the results and performance measures, it is observed that PSO-PI is producing better results than conventional PI controller.

*Index Terms*— Two-tank interacting process, PI controller and PSO-PI.

#### I. INTRODUCTION

The process industries require the liquids to be pumped, stored in tanks and then pumped to another tank. Many times the liquid will be processed by chemical or mixing treatment in the tanks, but always the level of the fluid in the tanks must be controlled. A level that is too high may upset the reaction equilibrium, cause damage to the equipment or result spillage of valuable or hazardous material [1]. If the level is too low, it may have bad consequences for the sequential operations. Hence, control of liquid level is an important and common in process industries. Conventional controllers are widely used in industries since they are simple robust and familiar to the field of operator. The most basic and pervasive controller algorithm used in the feedback control is proportional integral controller algorithm. PI controller is widely used control strategy to control most of industrial automation process because of its remarkable efficiency and simplicity. Hence, a mathematical model is derived and a simulation is carried out for the given mathematical equation. The conventional PI controller parameters are designed based on Ziegler-Nicholas. However, it will not give satisfactory response for change in operating point. Hence, the Particle Swarm Optimization technique is proposed and implemented to optimize PI controller parameters [4]. In this work, a simple performance criterion in time domain is proposed for evaluating the performance of a PSO-PI controller that is applied to a interacting two-tank process.

#### **II. PROCESS DESCRIPTION**

Fig.1 shows the photograph of the laboratory level process station. It consists of three pumps, two motorized control

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valves, six process tanks, two overhead tanks, two differential pressure transmitters, five level transmitters and rotameters .Instrumentation panel consists of two PID controllers, main power supply switch, pump switches, motorized control valve switches and auxiliary switches for individual components.

#### III. WORKING PRINCIPLES

Fluid level in the tank is measured by level transmitter (LT). Output of LT is given to the data acquisition setup. It consists of ADC and DAC. The differential pressure level transmitter (DPLT) measures the flow by sensing the difference in level between the tanks. The DPLT then transmits a current signal (4-20mA) to the I/V converter. The output of the I/V converter is given to the interfacing hardware associated with the personal computer (PC). Control algorithms are implemented in Lab view software. It compares and takes corrective action on the motorized control valve. Based on the valve opening flow rate is manipulated. Rotameter can visualize the flow rate.



Fig.1. Experimental setup of a two-tank interacting process.

The controller compares the controlled variable against set point and generates manipulated variable as current signal (4-20mA) [2]. Here the controlled variable is the level ( $h_2$ ) and the manipulated variable is the flow rate ( $q_{in}$ ).Specification dimension are tabulated in Table I and Table II ,respectively.

#### TABLE I

### SPECIFICATION OF TWO-TANK INTERACTING PROCESS

	COMPONENTS	SPECIFICATIONS
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MOTORISED	Flow rate	50LPH
CONTROL	Characteristics	Equal%
VALVE	Valve action	motorized
		control
	m	
ROTAMETER	Туре	variable area
	Range	(0-100)LPH
	float material	i.e (0-1666
		<sup>3</sup> /min)
		SS 316
PUMP	RPM	4500
	Discharge	1000(LPH)
	Voltage	220/230 volts
	0	AC&DC
PROCESS TANK	Capacity	3 litres
	Height	300 mm
	Diameter	120 mm
LEVEL	Input	24V DC
TRANSMITTER	Height	0-400 mm WC
	Туре	F capacitance
		*
DIFFERENTIAL	Input	0-400mm H <sub>2</sub> O
PRESSURE	Supply	24V DC
TRANSMITTER	Output	4-20mA at 24V
	*	DC

TABLE II DIMENSIONS AND VARIABLES FOR TANK1 AND TANK 2

Parameter	Dimension		
Area(A <sub>1</sub> ,A <sub>2</sub> )	113.0973 cm <sup>2</sup>		
Height(max)	25 cm		
Diameter	12 cm		
Inflow rate(MV),q <sub>in</sub>	0-1666 cm <sup>3</sup> /min		
Process Variable (PV),h <sub>2</sub>	0-25 cm		
Flow rate (LV),q <sub>L1</sub> ,q <sub>L2</sub>	0-500 cm <sup>3</sup> /min		
G	Gravity (9.81N/m <sup>2</sup> )		
a <sub>1</sub> and a <sub>2</sub>	Area of the pipe outlet $(a_1=3.5735cm^2, a_2=3.9012cm^2)$		
c <sub>d</sub>	Discharge co-efficient ( c <sub>d</sub> =0.08)		

MV- manipulated variable, PV-process variable LV-

Load variable **B**.

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Fig.2 shows the process consists of two interacting liquid tanks. The volumetric flow into the tank1 is  $q_{in}(cm^3/min)$ , the volumetric flow rate from tank1 to tank2 is  $q_1(\text{cm}^3/\text{min})$ , and the volumetric flow rate from tank2 is  $q_0(\text{cm}^3/\text{min})$  [2]. The height of the liquid level is  $h_1(cm)$  in tank1 and  $h_2(cm)$  in tank2 (cm), respectively Both tanks have the same cross sectional area  $A_1(cm^2)$  and  $A_2(cm^2)$ ,  $q_{L1}$  is the inflow of tank1 as load disturbance (cm<sup>3</sup>/min) and  $q_{L2}$  is the inflow of tank2 as load disturbance  $(cm^3/min)$  [1and 2].



tank1

Fig.2.Two-tank interacting process

Mass balance equation for tank 1

$$A_1 \frac{\mathrm{dh}_1}{\mathrm{dt}} = q_{in} - q_1 \tag{1}$$

Assuming non -linear resistance to flow :

$$q_1 = \frac{c_d a_1}{A_1} \sqrt{2g(h_1 - h_2)}$$
(2)

Mass balance equation for tank 2

$$A_2 \frac{\mathrm{dh}_2}{\mathrm{dt}} = q_1 - q_o \tag{3}$$

Assuming non-linear resistance to flow:

$$q_{o} = \frac{c_{d}a_{2}}{A_{2}}\sqrt{2gh_{2}}$$

$$A_2 \frac{dh_2}{dt} = \frac{c_d a_1}{A_1} \sqrt{2g(h_1 - h_2)} - \frac{c_d a_2}{A_2} \sqrt{2gh_2}$$
(4)

#### IV. CONTROLLER TUNING

#### A. Process reaction curve for two-tank interacting process

Fig.3 shows the simulated open loop response of interacting process. The level (h<sub>2</sub>) changes from 0 to 8.5 cm, when applying a step input in  $q_{in}(50*16.66 \text{ cm}^3/\text{min})$  also the level  $(h_1)$  changes from 0 to 18 cm due to interaction. The simulated process reaction curve(PRC) of h2 for step change in  $q_{in}$  for ±499.8cm<sup>3</sup>/min is shown in Fig.4.



**Fig.3.** Simulated open loop response of  $h_1$  and  $h_2$  of interacting Process.



**Fig.4.** Simulated PRC of  $h_2$  for step change in  $q_{in}$  for  $\pm 499.8 \text{ cm}^3/\text{min}$ .

From the fig.4 the transfer functions are obtained and tabulated in Table III. From the average transfer function, the controller parameters are obtained using Z-N tuning rule [2]. For two-tank interacting process the PI controller parameters are tabulated in Table IV.

# TABLE III TRANSFER FUNCTION MODEL OF TWO-TANK INTERACTING PROCESS

Step	<b>Transfer Function</b>	Average Transfer		
Input <b>q<sub>in</sub></b>		Function		
Positive Step	0.81578			
Input, <b>q</b> <sub>in</sub>	$93s + 1^{e}$	0.65049		
Negative Step	0.4852	$97.5s \pm 1^{e}$		
Input, <b>q</b> <sub>in</sub>	$\frac{102s+1}{102s+1}e^{-10s}$			

# A.Z-N tuning technique

Based on the average transfer function the value of  $k_{\rm c}$  and  $t_{\rm i}$  are calculated using Z-Ntechniques. The values of  $k_{\rm c}$  and  $t_{\rm i}$  are tabulated in Table IV.

### TABLE IV

# PI CONTROLLER SETTINGS FOR TWO-TANK

#### INTERACTING PROCESS USING Z-N METHOD.

Mode	K <sub>c</sub>	$T_i(sec)$
PI	7.9351	56.61

### C. Particle swarm optimization (pso) algorithm

Particle swarm optimization (PSO) algorithm, which is used for optimizing the PSO difficult numerical functions and based on metaphor of human social interaction, is capable of mimicking the ability of human societies to process knowledge [4]. It has roots in two main component methodologies: artificial life (such as bird flocking, fish schooling and swarming) and evolutionary computation. Although the PSO algorithm is initially developed as a tool for modelling social behaviour, it has been applied in different areas.



Fig.5. PSO based PI controller to control the level of

two- tank interacting process.

The block diagram of PSO based PI controller is shown in Fig 5. Also the flow chart to optimize the PI controller is shown in Fig 6.



The equation for position and velocity

 $\mathbf{V_{n+1}} = \mathbf{v_n} + c_1 \text{rand1}()^* (p_{\text{best,n}} \text{-current position}) + c_2 \text{rand1}( )^* (g_{\text{best,n}} \text{-current position})$  (5)

 $\mathbf{x} (\mathbf{t} + \mathbf{1}) = \mathbf{x}_{id} (\mathbf{t}) + \mathbf{v}_{id}(\mathbf{t} + \mathbf{1})$ (6)

# **D.** The PSO learning algorithm is represented by following steps

- Step1Select the number of iterations (n) and the PSO<br/>learning rate  $(c_1, c_2)$ .
- **Step2** Randomly generate position vector X and associated velocity V of all particles in the population.
- **Step4** For every particle, update its own velocity and position value.

Step5 If iteration=n, then go to exit, otherwise go to step 3.

**Step6** The best particle's value will be selected as the finial parameter set to form desired PI controller.

During simulation the values for PSO algorithm considered are tabulated in Table V.

TABLE V			
PARAMETER OF PSO ALGORITHM			
Parameter	Values		
Number of Iteration	20		

rumber of iteration	20	
Dimension	3	
Swarm Size	90	
Correction Factor	C <sub>1</sub>	1.2
	C <sub>2</sub>	1.4

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The optimized PSO-PI parameter using equation 5 and 6 are tabulated

 TABLE VI

 PARAMETERS OF PI AND PSO-PI CONTROLLERS

Mode	K <sub>c</sub>	$T_i(sec)$
PI	7.9351	56.61
PSO-PI	2.03791	0.1005

# V. SIMULATION RESULTS

A. Servo responses of level  $h_2$  with PI and PSO-PI controllers.

The servo responses for two tank level interacting process for step change in  $h_2$  from 6 to 8 cm, from 8 to 6cm is shown in fig.7 by implementing PI and PSO-PI. The corresponding change in  $h_1$  and inlet flowrate  $q_{in}$  are also shown in fig.8 and fig.9, respectively. The performance measures for step change in  $h_2$  from 6 to 8 cm is tabulated in Table VII. From the results and Table VII, it is observed that the PSO-PI gives better



**Fig.7**. Servo response of  $h_2$  with PI and PSO-PI controllers.





Fig 9. Response of PI and PSO-PI output qin for servo response.

**Fig.8**.Servo response of h<sub>1</sub> with PI and PSO-PI controllers.

# TABLE VII COMPARISON OF PERFORMANCE MEASURES LEVEL WITH PI AND PSO-PI FOR SERVO RESPONSE (6-8) CM

Servo response for h <sub>2</sub> (6-8)cm			
	t <sub>s</sub> (sec)	%overshoot	ISE
PI	1988	12.825	353.4
PSO-PI	978	33.66	254.2

# B. Regulatory response for Positive step change load variable $q_{L1}({\rm +})$

A sudden load disturbance of +10% is given in inlet flow rate of tank1 at 4000 sample from  $q_{L1}(+)$ . Due to this level in  $h_1$  increases for PI from 13.3 to 14.5 cm and PSO it increases from 13.3 to 15.4 as shown in fig.11. The level  $h_2$  also increases for PI from 6 to 6.5 cm and PSO it increases from 6 to 6.9cm as shown in fig 10. The PI and PSO-PI Controller takes necessary action to reduce the flowrate  $q_{in}$  from 420 to 350 (ref fig12) In order bring back the level  $h_2$  back to 6cm as shown in fig 10.



Fig 10. Regulatory response of  $h_2$  with PI and PSO due to load variation in +10% from  $q_{L1}$ .



Fig 11. Regulatory response of  $h_1$  with PI and PSO-PI due to Load variation in +10% from  $q_{L1}$ .



Fig 12. Response of PI and PSO output( $q_{in}$ ) for load variation in +10% from  $q_{L1}$ 

# C. Regulatory response for negative step change load variable $q_{L1}(-)$

A sudden load disturbance of -10% is given in inlet flow rate of tank1 at 4000 sample from  $q_{L1}(-)$ . Due to this level in  $h_1$  decreases for PI from 13.3 to 12.1 cm and PSO it decreases from 13.3 to 11.1 as shown in fig 14. The level  $h_2$  also decrease for PI from 6 to 5.5 cm and PSO it decreases from 6 to 5.1 cm as shown in fig 13. The PI and PSO-PI Controller takes necessary action to increase the flowrate  $q_{in}$  from 425 to 500 (ref fig 15) in order bring back the level  $h_2$  back to 6cm as shown in fig 13.



Fig 13. Regulatory response of  $h_2$  with PI and PSO-PI due to load variation in -10% from  $q_{L1}$ 



Fig 14. Regulatory response of  $h_1$  with PI and PSO-PI due to load variation in -10% from  $q_{L1.}$ 



Fig 15. Response of PI and PSO-PI output  $(q_{in})$  for load variation in -10% from  $q_{L1}$ .

TABLE VIII COMPARISON OF PERFORMANCE MEASURE OF LEVEL WITH PI AND PSO FOR REGULATORY RESPONSE.

Regulatory Response h <sub>2</sub> (6-8)cm					
Controller	+10% from $q_{L1}$ -10% from $q_{L1}$				
	t <sub>s</sub> (sec)	ISE	t <sub>s</sub> (sec)	ISE	
PSO-PI	1032	2822	1046	2821	
PI	1460	9316	1275	9316	

# D. Regulatory response for positive step change load variable $q_{L2}(+)$

A sudden load disturbance of +10% is given in inlet flow rate of tank1 at 4000 sample from  $q_{L2}(+)$ . Due to this level in  $h_1$  increases for PI from 13.3 to 13.5 cm and PSO it increases from 13.3 to 13.6cm as shown in fig 17. The level  $h_2$  also increases for PI from 6 to 7 cm and PSO it increases from 6 to 6.9cm as shown in fig 16. The PI and PSO-PI Controller takes necessary action to reduce the flowrate  $q_{in}$  from 420 to 200 (ref fig18) in order bring back the level  $h_2$  back to 6cm as shown in fig 16.



Fig 16. Regulatory response of  $h_2$  with PI and PSO-PI due to load variation in +10% from  $q_{L2}$ 







due to load variation in +10% from  $q_{L2}$ .

# E. Regulatory response for Negative step change load variable $q_{L2}(-)$

A sudden load disturbance of -10% is given in inlet flow rate of tank1 at 4000 sample from  $q_{L2}(-)$ . Due to this level in  $h_1$  increases for PI from 13.3 to 15.6 cm and PSO it increases from 13.3 to 15 as shown in fig 20. The level  $h_2$  also decreases for PI from 6 to 5.6 cm and PSO it decreases from 6 to 5.8 cm as shown in fig 19. The PI and PSO-PI Controller takes necessary action to increase the flowrate  $q_{in}$  from 420 to 750 (ref fig21) in order bring back the level  $h_2$  back to 6cm as shown in fig 19.



Fig 19. Regulatory response of  $h_2$  with PI and PSO-PI due to load variation in -10% from  $q_{L2}$ .



Fig 20. Regulatory response of  $h_1$  with PI and PSO-PI due to load variation in -10% from  $q_{L2}$ .



Fig 21. Regulatory response of  $q_{in}$  with PI and PSO-PI due to load variation in -10% from  $q_{L2}$ .

### TABLE IX COMPARISON OF PERFORMANCE MEASURE OF WITH PI AND PSO-PI FOR REGULATORY

Regulatory Response h <sub>2</sub> (6-8)cm					
Controller	+10% f	rom q <sub>L2</sub>	-10% fı	rom q <sub>L2</sub>	
	t <sub>s</sub> (sec)	ISE	t <sub>s</sub> (sec)	ISE	
PSO-PI	1036	2824	1045	2826	
PI	1460	9321	1277	9311	

# VI. CONCLUSION

The non-linear mathematical model of a two-tank interacting process was derived. To improve the performance of closed loop control a PSO-PI was designed and implemented for a two-tank interacting process. The servo and regulatory responses were obtained with PSO-PI. The performances of PSO-PI were compared with that of conventional PI controller in simulation. The performance measures were tabulated. It is observed that the PSO-PI gives is better performance on terms of less integral square error, faster settling time and without oscillation.

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