Statistical modeling of entire prime numbers

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Abstract—Shown incomplete Gaussian number of primes. On infinite number of integers proposed finite-dimensional rows with the same (symmetrical rows) or different (asymmetric series) power on negative and positive (real) numbers. The center of symmetry of a symmetric number of the whole prime numbers concerning number 0 is reasonable. The row axis, its geometrical variations and parameters depending on number of couples of prime numbers are shown. The criticism of application of a natural logarithm for calculation of power of a number of prime numbers is given, and also the characteristic of a centuries-old psychological barrier at mathematicians and errors of approximation of ranks of prime numbers are shown.

Are methods of identification of steady laws of distribution of the whole prime numbers and the analysis of the revealed wave functions of parameters of the provision of an axis at their symmetric ranks are given.

Index Terms—integer primes, symmetrical rows, geometry from power, kernel and center, parameters, symmetry axis, wave regularities.

1. INTRODUCTION

In 2200 and more years, a known number of prime numbers considered as a firm design [14]. However, as we will show further, known ranks of prime numbers appeared only special cases. Thus the mathematical description for the whole prime numbers even became simpler. There was also accurate geometrical interpretation of different symmetric and asymmetric ranks of the whole prime numbers.

It is interesting to note that to 15-year-old Gauss presented the book on logarithms with the appendix of a number of prime numbers which began with 1 [14]. This series of prime numbers, starting with the unit, was shown in one of the films on the history of mathematics. But as an adult Gauss removed 1, and began to count the series since number 2. It is a simplification of series we believe the reason that long Gauss did not publish their results on the analysis of power series. Thus he walked away from the series itself, and began to count the number of prime numbers in the tens, hundreds, thousands, etc., that achieve planned by it still as age 15, well-known law of prime numbers. Subsequently Riemann (2, 3, 5, 7, 11 ... and we have left. The authority of the Gauss still so great that this inaccuracy of mathematics is still not taken into account. In the end, all is considering only asymmetric set consisting only of positive primes.

It is necessary to remember that Einstein was not fond of negative numbers and never used them. In the end, the psychological barrier of counter-making and also negative integers was very great. Therefore, all mathematicians have done not by a series of Prime numbers, but only the capacity of the truncated series that begins with 2.

Criticism of the use of the natural logarithm. Gauss, Riemann, and after them other mathematicians became interested in the relative power \( x/\pi(x) \) of the number of prime numbers with a truncated beginning (without 0 and 1, that is, of the series was discarded a whole system binary notation).

At that numbers always are presented only in a decimal numeral system.

But, as we understood in the publications [4-9], it is necessary to pass to a binary numeral system. Thus we understood one: the person considers in decimal, and the nature – in binary numeral systems. As a result many unclear to mathematics of property of a number of prime numbers (for example, jumps of numbers in some places of a row) appeared simply on borders of blocks of binary notation.

Apparently, unconsciously, this indicator of relative power of a number of prime numbers \( x/\pi(x) \) was a logarithmic with the irrational basis \( e = 2.71... \). Here youth and Gauss’s talent affected. However, thereby, upon transition from degree of ten to its natural logarithm, there was a so-called false identification. It also became the main mistake in the analysis of prime numbers when Gauss passed from the row to occurrence of prime numbers according to categories of a decimal numeral system.

Application \( \ln 10 \) brought in mathematical transformations to false for a number of natural numbers (and incomplete at first 0 and 1) idea. This idea assumes that in the subsequent categories of decimal system quantity of prime numbers all the time increases approximately on 2.3.

Proceeding from this idea, adopted the law of prime numbers, that \( \pi(x) \sim \lfloor x/\ln x \rfloor \).

The reason of such turn in studying of prime numbers was very trivial. As it is noted in article [14]: «Gauss, the greatest mathematician, discovered the law \( \pi(x) \sim \lfloor x/\ln x \rfloor \) at the age of fifteen, studying the table of prime numbers, contained in given him the year before the table of logarithms». This commitment young Gauss was unshakable in the theory of prime numbers the next two centuries.

We have abandoned the use of the natural logarithm of 10. Then have passed to binary notation [7]. However it appeared that a traditional number of prime numbers is insufficiently correct at first 0 and 1. This incorrectness became more noticeable after cutting off of a so-called gain from the most prime number. The main shortcoming is that there is no negative half shaft here. Therefore a Gaussian number of prime numbers was asymmetric, located out of the beginning of a positive half shaft of natural numbers.

The contradiction between accident and regularity arises from the record of prime numbers in a decimal numeral system. Doesn’t help but only confuses, transition to a logarithmic scale with the basis of number of time \( e = 2.71... \). More precisely: the logarithmic scale of notation takes away from an essence of a number of prime numbers.
II. STRONG PSYCHOLOGICAL BARRIER

Gauss and its number of prime numbers long prevailed and over our thinking. But the first attempts of overcoming of a psychological barrier appeared already in [4].

Experience of inventive activity in equipment and technology, and also application in physical and mathematical researches of the strong theorem of Gödel about incompleteness, allowed to receive the first result which is stated in this article.

A number of prime numbers studied since Euclid without 0 and 1 we called a traditional row \(a(n) = \{2, 3, 5, 7, 11, 13, 17, \ldots\}\) with order (serial number) \(n = \{1, 2, 3, \ldots\}\), which was considered by Gauss, Riemann and many others. But it appeared that serial number doesn’t make essential substantial sense. Most important a dissonance or compliance between ranks \(a(n) = \{2, 3, 5, 7, 11, 13, 17, \ldots\}\) and natural numbers \(N = \{0, 1, 2, 3, 4, 5, 6, \ldots\}\).

Their detailed factorial and statistical analysis in the program environment CurveExpert [12] showed that there complete series of prime numbers \(P = \{0, 1, 2, 3, 5, 7, 11, 13, 17, \ldots\}\) on a positive half shaft of system of the Cartesian coordinates [5], equipotent to a number \(N = \{0, 1, 2, 3, 4, 5, 6, \ldots\}\) of natural numbers. The complete series is displayed on two unequal parts: 1) finite-dimensional number of critical prime numbers \(P = \{0, 1, 2\}; 2) noncritical prime numbers \(P = \{3, 5, 7, 11, 13, 17, \ldots\}\) in the form of an infinite-series. It shares in a different way also on: 1) elements of system of binary notation 0, 1; 2) traditional row \(a(n) = \{2, 3, 5, 7, \ldots\}\).

Among the whole prime numbers these structures remain.

The confidence of new scientific results after transformation of prime numbers in binary codes allowed to approach to consideration of the main question of the new theory - physical sense of growth of relative power of a number of prime numbers [5, 8].

III. BRIEFLY ABOUT IDENTIFICATION METHODOLOGY

Basic and well-defined view of the theory of prime numbers are positive integers in area \((0; \infty)\).

If the number \(j\) of natural numbers also be taken as a number of natural numbers \(N = \{0, 1, 2, 3, 4, 5, 6, \ldots\}\), that any natural number will be determined by the expression \(N_{j+1} = N_j + 1\).

The increase in natural numbers is always equal to one. Then we notice that any rank distribution is sequence any measured or otherwise obtained quantitative data on decrease or increase certain physical (the term in a general sense) ordinates as displays of any real phenomenon or process along abscissa axis.

Moreover, the abscissa axis is always becoming a full range of natural numbers.

In a general sense any ordinate concerning number \(n\) separate fragments or completely belongs to a number of natural numbers. But in this case violated the order members primes regarding the adopted order \(j\).

As a result the nonlinear order \(n \neq j\) on a positive half shaft of the abscissa, not coinciding with is established by ordinate.

IV. ABOUT NUMERICAL SYSTEMS

For the hierarchy between sets of numbers known expression [2, 11]:

\[
P \subset N \subset Z \subset Q \subset R \subset C.
\]

The first two systems (prime and natural numbers) in our case are built in third (integers). Earlier [5] we lowered a type of integers of \(Z\), because of rejection of negative numbers, even in a complete series of positive prime numbers \(P = \{0, 1, 2, 3, 5, 7, 11, 13, 17, \ldots\}\). Therefore in the statistical analysis [4, 5] from prime numbers \(P \subset N\) in [5] there was a jump to the real (real) numbers according to the scheme \(P \subset N \subset R \subset C\).

Moreover, the patterns are identified without regard to complex numbers \(C\), but necessarily irrational numbers type \(e = 2.71\ldots\) (number of time) and \(\pi = 3.14\ldots\) (number of spaces). In software environment CurveExpert accepted [10] 18 decimal places. It allows to compare regularities of a complete series of prime numbers to other fundamental physical constants [6].

Complicating the theory from [5], we accept from the scheme on a formula (1) and integers \(Z\).

Then for the whole prime numbers the hierarchy (1) is given to the look scheme

\[
P_n (P \subset N) \subset Z \subset Q \subset R \subset C.
\]

In the beginning there is a group \(P_n \leftarrow \pm(P \subset N)\), and then jump \(P_n \subset Z \subset R\).

Thus rational numbers from a set \(Q\) appear automatically, in the form of the actual (real) numbers \(R\), for example 0,5 \ldots or 1/2 at the proof of a hypothesis of Riemann [5, 8].

V. INITIAL PREREQUISITES OF THE WHOLE PRIME NUMBERS

Natural numbers \(N = \{1, 2, 3, \ldots, \infty\}\), received at the natural account, from the basic become a supportive application. Then a known number of the prime numbers (PN) has an appearance \(P = \{1, 2, 3, 5, 7, 11, 13, 17, \ldots, \infty\}\). Thus we refuse a Gaussian number of a look 2, 3, 5, 7, 11, \ldots.

In these systems \(N\) and \(P\) finite-dimensional traditional ranks will register as sequence \(P_n = \{1, 2, 3, 5, 7, 11, 13, 17, \ldots\}\).

It is known that association of natural numbers with zero and negative numbers gives system of integers of a look \(Z = \{-\infty, \ldots, -2, -1, 0, 1, 2, \ldots, \infty\}\).

Then number 0 becomes the center for a symmetric number of the whole prime numbers. Thus on abscissa axis the uniform scale is formed \(Z = \{0, \ldots, -1, 2, 1, \ldots, \infty\}\), always from the beginning of coordinates \(z = 0\).

Then finite-dimensional symmetric ranks of prime numbers will written \(P_z = \{-P_n, 0, P_n\}\).
Prime numbers within natural numbers are known since the time of Euclid and therefore the history of studying of their properties totals more than 2200.

Thus, the prime number is the natural number \( N = \{0,1,2,3,4,5,6,...\} \) having two natural dividers: unit and itself [14]. In the complete series of natural and prime numbers, we use all the numbers, including 0 as the first number. In this second requirement about simplicity, i.e. division by itself, is redundant, since all integers divisible by themselves. Therefore in the most correct definition of a prime number there is the only rigid requirement – division only on unit. It removes also mathematical problem of the uncertain relation in the form of division of zero into zero.

The reason for non-inclusion in the list of zero primes in the brochure, donated by 15-year-old Gauss, is to ignore the mathematicians in Europe digit 0 as such.

Up to the XIX century in Europe didn't know number 0, and in the middle ages its even mathematicians simply didn't recognize many. Therefore it isn't surprising that figure 0 wasn't included in a row prime numbers. And that is why 1 has been excluded from a number of Gauss prime numbers? We didn't find about this fact of historical data from the biography of the great mathematician though it was known also to Gauss from the brochure presented to it that all numeral systems are based on unit and a number of prime numbers to it also began with unit.

PN properties automatically pass and to WPN. Addition is creation round zero couples of PN with signs \( \pm \). Then power at finite-dimensional ranks of PN and WPN coincide on symbolical designation of couples \( n \) with different signs. Number 0 (further examples will show its special function or as a certain point of singularity) doesn't get to recalculation. Therefore it is impossible to extrapolate mathematical regularities of a number of PN or WPN on zero on a scale of abscissa: there is an uncertainty.

VIII. FINITE-DIMENSIONAL NUMBER WPN

We will review an example of a final number of WPN (table 1). This example was made in the computational capabilities of the software environment CurveExpert [12].

<table>
<thead>
<tr>
<th>Left edge</th>
<th>Center of symmetry</th>
<th>Right edge</th>
</tr>
</thead>
<tbody>
<tr>
<td>(-16500)</td>
<td>(-182057)</td>
<td>(-3)</td>
</tr>
<tr>
<td>(-16499)</td>
<td>(-182047)</td>
<td>(-2)</td>
</tr>
<tr>
<td>(-16498)</td>
<td>(-182041)</td>
<td>1</td>
</tr>
<tr>
<td>(-16497)</td>
<td>(-182029)</td>
<td>0</td>
</tr>
<tr>
<td>(-16496)</td>
<td>(-182027)</td>
<td>(\ldots)</td>
</tr>
<tr>
<td>(-16495)</td>
<td>(-182011)</td>
<td>2</td>
</tr>
<tr>
<td>(\ldots)</td>
<td>(\ldots)</td>
<td>3</td>
</tr>
</tbody>
</table>

In a series of prime numbers absolute power \( n \) shows the total number of nonzero members, and in the number WPN - number of couples of whole prime numbers. Power of WPN will be equal \( 2n \).

At total number \( 2n + 1 \) in table 1 example together with zero is \( 2 \times 16500 + 1 = 33001 \) whole prime numbers. Any
more isn’t located in memory of the program CurveExpert environment.

The beginning of coordinates accurately is defined in a point \( (Z = 0, \ P_z = 0) \). This is - the point of singularity, because under the existing definition of a prime number (property division by itself) is the division of a prime number to itself, i.e., 0/0.

Thus division only on 1 turns this point into zero.

The center of symmetry is defined by seven whole prime numbers. Thus to the left the half shaft 0, -1, -2 and -3 …, and to the right - a half shaft 0, 1, 2 and 3 … goes.

Signs give as we believe, an arrow of time of Stephen Hawking from left to right and, apparently, at the same time define a chirality of biological objects (in [5] us compliance of a number sequence of Fibonacci to a complete series of positive prime numbers was proved).

We will notice also that by results of researches [5] members 0, 1 and 2 treat in a complete series critical prime numbers. They didn’t allow mathematics more 2200 to find the distribution law in a traditional number of PN 2, 3, 5, 7, 11, … But Gauss one critical number 1 nevertheless cleaned, however number 2, apparently, didn’t dare to exclude. In a film on the history of mathematics is one of the famous mathematicians stated that his favorite number is 2, since it is the only even number in the series of prime numbers. But now we can say that in a series of even numbers 0, 1, 2, 3, 5, … even two - zero and deuce. And the scale of integers such even numbers even three: -2, 0, 2.

A noncritical number of prime numbers begins with number 3 [5] and it allows to reveal high-adequate mathematical regularities.

The sign doesn’t change essence of numbers but only correlates them to different “worlds” (negative and positive) therefore it is symmetric on the left half shaft 0,-1,-2,-3, …, -∞ also critical prime numbers 0,-1,-2 and-3 settle down at the left. Therefore a noncritical negative row -Pz begins with number-3.

Advancing contents of the subsequent articles and sections of this article, we will note that the physical analog of the horizon of events is on border of the sphere -1, 0, +1 from within (in the table 1 kernel of the center of symmetry is allocated), that is under a condition \( \pm P_z \rightarrow 1 \). And the rational number 1/2, or the valid root of dzeta-function of Riemann (on Riemann's known hypothesis or Gilbert's 8th problem) is a cross-cutting.

This root appears when transfer prime numbers from a decimal numeral system in binary system [5], and Riemann’s critical line accurately is defined at shift relatively by each of other two series of the whole prime numbers.

The geometry and patterns at different ranks of positive prime numbers were shown in [5].

IX. CENTER OF SYMMETRY OF A ROW WPN

In figure 1 the center schedule from seven points is shown. The schedule was received in the program CurveExpert-1.40 [10] environment and it is unambiguously identified by simple function

\[ P_z = Z, \ Z = -3, -2, -1, 0, 1, 2, 3. \]  \( \quad (4) \)

The same proporcionality is observed at the power of couples whole prime numbers \( n = 1 \sqrt{2} \sqrt{3} \) or the total number of members of a number of WPN \( 2n + 1 = 3, 5, 7 \).

Thus, in the symmetry center prime numbers (their quantities also prime numbers) coincide with values of elements of a scale of integers.

This center of symmetry is invariable at any power of a number of WPN, including and a condition \( n \rightarrow \infty \) at Cantor understanding of types of infinity, and it is a peculiar start of change of disproportion. Start happens from the proporcionality coefficient, equal 1, and proceeds indefinitely.

In a spherical cover of the center of symmetry (1 cover is in the table behind the allocated kernel) there are three fundamental constants (harmony and time number) – a gold and silver proportion, and also Napier’s number.

Thus, from a point of singularity 0 there is difficult and while mathematically an unclear expansion to border of a kernel [-1, 0, +1]. Then in a spherical cover [-3,-2, …, 2, 3] there is a jump of harmony [6] through number of time (table 2). As a result of WPN property unite achievements of physics and mathematics. The preliminary (working) hypothesis of association of four fundamental forces is given in [5, 6].

The gain of PN \( p_j \) or WPN \( p_z \) is formed when the second row moves on one position equal 1, and then we will receive formulas:

\[ p_j = p_j - p_{j+1}; \ p_z = p_z - p_{z+1}. \]  \( \quad (5) \)

Physically the gain of PN (table 2) is represented in the form of steps at Riemann’s ladder when these steps are isolated from the most triangular case of a ladder.

<table>
<thead>
<tr>
<th>Prime number</th>
<th>Increase PN</th>
</tr>
</thead>
<tbody>
<tr>
<td>( p_j )</td>
<td>( p_j )</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>2.41421</td>
<td>1.35914</td>
</tr>
<tr>
<td>2.71828</td>
<td>1.61873</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>5</td>
<td>2</td>
</tr>
</tbody>
</table>

In detail types of a gain and its geometry are shown in the book [5]. Thus for a gain a number of prime numbers becomes axis.
number of harmony (golden ratio) \( \varphi = (1 + \sqrt{5})/2 = 1.61803… \).
- number of harmony of beauty (silver section) \( e/\varphi = 2.41421…; \)
- half of number of time (Napier’s number) \( e/2 = 1.35914… \).

After parametrical identification of the law of achievement of a limit or the known law of distribution of Weibull in the form of a formula

\[
y = y_{\max} - a \exp(-bx^\gamma)
\]

was obtained (Fig. 2) binomial statistical regularity

\[
p_{y_{\max}} = 2 - 1.02402 \exp(-0.00025750 P_{n1,2,3,5}^{0,1,2,3,5}) . \tag{7}
\]

The same formulas in a general view are valid, at the accounting of the sign “minus” and repeated parametrical identification, and for a negative half shaft of a number of the whole prime numbers. Then harmony at any ranks of the whole prime numbers begins with \( \pm 3 \).

![Fig. 2. Gain jump from 1 to 2 in a complete series positive prime numbers](image)

This spasmodic transition gives anomaly in the mathematical equations of the law of distribution of prime numbers. Rejections of the schedule from points in figure 2 on a formula (7), as well as in other examples of modeling by identification of steady laws, occur because of the accuracy of acceptance of irrational number \( e = 2.71828… \) (only 18 signs in the mathematical CurveExpert-1.40 environment) and other fundamental physical constants. For an illustration in a formula (7) and others it is enough to specify values of parameters of model with 5 significant digits.

Due to the complexity of formalizing the core and the periphery of the centre of symmetry Gauss, followed by Riemann and other mathematicians, refused analysis alignments, and proceeded to recount them in decimal digits.

All went on the way of detection of the law of change of quantity at prime numbers in categories of a decimal numeral system. For this purpose passed into a numeral system with the basis of a natural logarithm, thus process of studying of prime numbers finally came to a standstill scientific progress in the theory of numbers.

It is a craze of linearization of obviously nonlinear ranks of statistical data. Therefore there was Gilbert’s which hasn’t been solved still 23rd problem when from Gauss’s “easy” hand was created the mathematical statistics on the basis of the so-called normal law of distribution ….

A series of WPN easily overcomes mathematical obstacles of two jumps (from number 0 to 1 and then from number 2 to 3) that in process of growth of power of couples of prime numbers there is in the beginning a recession of adequacy of identification by [10] steady laws, and then the coefficient of correlation increases, coming nearer under a condition \( n \to \infty \) again to 1.

### X. PERIPHERY OF A SERIES WPN

In this article, we consider only one series of integers prime numbers. If a symmetry center is a group of seven simple integer numbers in a finite series \( P_{z0} = [-3, -2, -1, 0, 1, 2, 3] \), then the entire infinite series WPN contains two private infinite-dimensional sequences - left semi-row \( -P_{z<1} \) and right semi-row \( P_{z>3} \).

The linearity of the basic law distribution of a series WPN any power geometrically interpreted as follows. The left and right private ranks of the whole prime numbers form a peculiar core of all design of distribution, passing special characteristics of the sphere -1, 0, +1 and spasmodic transition to harmony in a cover -3, -2, …, 2, 3. In a triad -1, 0, +1 are while distinctive signs unknown to us. In a spherical cover [-3, -2, …, 2, 3] there is a quantum leap from singularity for harmonious distribution from a prime number \( \pm 3 \) in two noncritical rows \( \pm P_{n=3,5,7,11,…} \).  

### XI. POWER INFLUENCE COUPLE OF WPN

Schedules of ranks of WPN are given in figure 3 at the power of couple prime numbers of 10 and 10000.

On these ranks from figure 3 the private equations of the law of prime numbers were received:
- for a row WPN \( n = 10 \) couple of prime numbers

\[
P_{z10} = 1.98182Z ; \tag{8}
\]

- for a row WPN \( n = 100 \) couple of prime numbers

\[
P_{z100} = 4.87381Z ; \tag{9}
\]

- for a row WPN \( n = 1000 \) couple of prime numbers

\[
P_{z1000} = 7.53273Z ; \tag{10}
\]

\( n = 10000 \) couple of prime numbers

\[
P_{z10000} = 10.10516Z . \tag{11}
\]
Fig. 3. Schedules of finite-dimensional ranks of the whole prime numbers (in the right top corner: $S$ - dispersion; $r$ - correlation coefficient)

Adequacy of which were detected linear patterns is very high, in excess of the correlation coefficient (a measure of closeness of the connection, given automatically) over 0.999.

XII. FUNDAMENTAL LAW OF DISTRIBUTION OF WPN

On the basis of induction on a set of partial examples generally it is possible to submit the law of distribution of WPN in the form of mathematical expression

$$P_Z = a(n)Z,$$

where $a(n)$ - coefficient of an inclination of an axis of symmetry of a series of power $n$ couple WPN.

This basic parameter any series of WPN has a clear geometric meaning.

The relation of a prime number (ordinate) to the integer (abscissa) gives a tangent of angle of an inclination $\alpha$ of an axis of symmetry at any number of WPN to abscissa axis $Z$ on a formula

$$tg \alpha = P_Z / Z = a(n).$$

From expression (12) and graphics in figure 1 we notice that the lower bound of a tilt angle of an axis of symmetry becomes $45^\circ$ or $\alpha_{\min} = \pi/4$. Under a condition $n \to \infty$ will be also $P_Z \to \infty$, therefore $\alpha_{\max} = \pi/2$. Then the interval of change of coefficient of an inclination at an axis of symmetry will be equal $a(n) = [1, \infty)$, and the interval of a tilt angle of an axis will change in limits $\alpha = [\pi/4, \pi/2]$.

XIII. LIMIT OF THE PROGRAM ENVIRONMENT ON THE POWER OF THE WPN

The program environment allows to contain only slightly more than 33000 values (lines) of basic data (Fig. 4).

After parametrical identification the formula was received

$$P_{Z_{16500}} = 10.65994Z.$$  

(XIV. PHYSICAL INTERPRETATION)

Point distribution of the remains (fig. 5) shows similarity to pair sleeves of spiral galaxies. But such comparison demands search of statistical regularities in concrete measurements of parameters from a set of galaxies. Such basic data are necessary to us.

XV. IDENTIFICATION HEURISTIC

We selected the previous distinctive signs of WPN after performance of process of identification when received geometrically beautiful on a design private models from the fundamental law of an axis of symmetry of WPN with very high level of adequacy at correlation coefficient more than
0.999. Basic data of table 1 have no measurement errors. Therefore they are absolutely reliable, sound and reliable.

But we were initially sure of successful result as soon as the inspiration came and understood asymmetry of any number of positive prime numbers from our book [5]. Then when modeling from the existing theory of approximation there are two stages - a choice of a type of the equation (people) and search of values of its parameters (computer).

However we completely refused long ago from approximation and, respectively, at all we don't apply the statistics program from Excel, and developed methodology of identification [10]. In the new theory the first stage is excluded from the theory of approximation because steady laws are in advance set, and from them is it possible to create various mathematical constructs. Use in each case of statistical (probabilistic) modeling of this or that steady law (according to table 3 of their seven) demands heuristic judgment of the maintenance of a problem of modeling.

Thus, at heuristic level Gilbert's 23rd problem (development of methods of calculus of variations) while is insufficiently solved by us. But it is almost solved at structural and parametrical levels of the analysis and synthesis. The variation of functions is reduced to conscious selection of steady laws and designing on their basis of adequate steady regularities. Such confidence was reached by tens of thousands of examples of mathematical (statistical) modeling by identification.

In relation to wave indignations of oscillatory adaptation of considered system (finite-dimensional symmetric and asymmetric ranks of the whole prime numbers appeared statistically representative selections) in this article we will note only two new physical and mathematical features (structural and parametrical identifications).

XVI. IDENTIFICATION STRUCTURAL

Descartes assumed existence of the one and only algebraic equation suitable as version of the decision for any types of the integrated equations. Hilbert dreamed of invariants from which as from bricks this universal equation will gather. Our universal invariants are given in table 3.

Table 3. Mathematical constructs in the form of stable laws to build a statistical model

<table>
<thead>
<tr>
<th>Table 3. Mathematical constructs in the form of stable laws to build a statistical model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fragments without previous history of the phenomenon or process</td>
</tr>
<tr>
<td>[ y = ax ] - law of linear growth or decline (with a negative sign in front of the right side of this formula)</td>
</tr>
<tr>
<td>[ y = ax^e ] - exponential growth law (law of exponential death ) [ y = ax^e ] is not stable because of the appearance of infinity at zero explanatory variable</td>
</tr>
<tr>
<td>[ y = ax e^{(-cx)} ] - biotech law (law of life skills) in a simplified form</td>
</tr>
</tbody>
</table>

They are grouped in the principle "from simple to difficult". In fact, fragments and the biotechnical law are "Hilbert's bricks" for construction, during process of structural and parametrical identification, an additive design of required statistical model with trends and wavelets. Invariants of oscillatory indignations in the form of asymmetric wavelet-signals also include constructs from table 3 as amplitude (half) and a half-cycle.

In table 3 the most meeting invariants (fragments) are shown. At them ahead can be located operational constants \( \leftrightarrow \) or \( \leftrightarrow \). Six stable distribution laws are special cases of biotech law, shown at the bottom of table 3. In the title of the law the word "biotechnical" means that we adhere to the ideas of V.I. Vernadsky about the space of the functions of life. This is proved [5] by the fact that the Fibonacci series is a kind of "relative" of a number of positive primes. If you know the background of the formation of heuristic numeric field (table model), it is quite possible semantic decoding each wavelet signal whose wavelet (wave function) in its design contains certain mathematical invariants from table 3.

All known laws of distribution are particular cases of the biotech law that is shown in detail in the tutorial.

For example, the law of Gauss of so-called normal distribution will register from the law exponential (on the basis with time number) death according to table 3 with addition with the fourth parameter of model in the form of a formula

\[
y = a \exp(-c(x-e)^{d-2}) , \quad e = \bar{x} .
\]

Stable laws and the laws based on them make the selection equation for identification on statistical data (numeric fields) is quite meaningful, and therefore probabilistic modeling is only at random search software environment CurveExpert type values in the desired model. Therefore, identification of the theory first stage (selection of random structure of the equation) is excluded and only the second stage - the random identification of the model parameters.

Identification of the structure of the model is carried out by treating the initial data as follows:
- first identify deterministic nonlinear patterns;
- then add to these trend patterns vibration disturbances.

XVII. PARAMETRIC IDENTIFICATION

It was performed in a software environment CurveExpert-1.40 and information identification technology used by students (future bachelors and masters), as well as graduate and doctoral students.

On the methodology through examples structural-parametric identification is shown in detail in the book [5].

Selecting the desired model of the structure, which is an algebraic solution for the unknown Descartes primitive by wave equations having variable amplitude and half-life (half the frequency as the inverse of the half-period) oscillatory perturbation of the research object is made of stable laws (invariants), shown in table 3.

Process of parametrical identification automatically stops on a condition of achievement of parameters of model of some minimum increment and stops the user at achievement by designed model of an error of measurements.

XVIII. LEVELS OF ADEQUACY OF REVEALED REGULARITIES

Table 4 shows the ranges of the correlation coefficient as a
measure of the adequacy of the model.

The existing range of quantification closeness of the connection between the factors taken (no communication, weak and strong coupling) is very rude.

Criterion (a quantitative measure) identification becomes a measurement error in the preparation of a number field, i.e. table source data for other phases of identification. For example, prime numbers and their series [5] no have error measurement error: they are absolutely reliable, high-quality and reliable. Other types of basic data have different original error. Thus, numerical mathematical objects - to identify the best law-invariants.

In second place are precision measurements in astronomy, physics, engineering and technology and other fields of science. In third place stand biological objects (we - the trees), and their behavior has clearly manifested an oscillatory character, so linear and linear zed models biologists do not fit. The highest error are socio-economic dimensions because of their high subjectivity.

Therefore, we have proposed for technical experiments, in which the measurement error does not exceed 5%, the other scale (the third column of table 4).

However, it became clear that the scale levels of adequacy is also insufficient.

For many natural (biological) objects and results precision physical measurements had to introduce two interval adequacy level of the fourth column of table 3, that the world was made only in the simulation distributions series primes [5]. And for genetic engineering, according to article 1, we had to introduce another level of adequacy, which we opened only for whole series of integers prime.

XXI. Asymmetric wavelet

We adhere to Descartes's concept about need application of the algebraic equations directly as final mathematical decision, and without application of antiderivatives (the differential and/or integrated equations). We offered a new class of wave functions [4-9].

Conditions wavelets [1] fully satisfies asymmetric wavelet function of the form

\[
y = \sum_{j=1}^{m} y_j,
\]

\[
y_j = a_{j0} x^{a_{j1}} \exp(-a_{j2} x^{a_{j3}}) \times 
\times \cos(\alpha \xi /a_{j5} + a_{j6} x^{a_{j7}} \exp(-a_{j8} x^{a_{j9}}) - a_{j10}),
\]

where \( y \) - indicator (dependent factor), \( i \) - number of component (6.3), \( m \) - quantity of components, \( x \) - explanatory variable (contributing factor), \( a_{j0}, ..., a_{j10} \) - the parameters accepting numerical values during structural and parametrical identification (18).

The formula (18), in fact, is the algebraic equation to which Descartes aspired.

In most cases for identification of required regularities the truncated design (on a formula of frequency of fluctuation) asymmetric wavelet of type is sufficient.
Thus the separate geometrically organized pieces from a series of prime numbers, in particular on borders of distribution of amplitude wavelets, characterize a certain algorithm of behavior of individuals and their populations in time and space.

XXIII. SCALE OF COUNTING OF POSITIVE PRIME NUMBERS

In the Gaussian theory of prime numbers at calculation of relative power of prime numbers according to categories of a decimal numeral system decimal and logarithmic scales are applied.

Our recommendation [5] «not to change a scale of counting of prime numbers» in researches on the theory of prime numbers recognizes that, since Gauss and Riemann, apply a natural logarithm and look for an empirical formula of relative power of prime numbers in categories of a decimal numeral system.

Fully quote from the publication of Don Zagier [14].

«It is visible that the relation \( x \) to \( \pi(x) \) upon transition from this degree of ten to the subsequent all the time increases approximately on 2,3. Mathematicians learns at once among 2,3 logarithm 10 (certainly, on e basis e). The assumption results that \( \pi(x) \sim \log x \), and the sign ~ means that the relation of the expressions connected by it with growth \( x \) aspires to 1. This asymptotic equality for the first time published in 1859, is called now as the law of distribution of prime numbers. Gauss, greatest of mathematicians, opened this law at fifteen-year age, studying the tables of the prime numbers containing in presented to it in a year before to the table of logarithms».

XXIV. VERIFICATION OF THE LAW OF GAUSS

We weren't too lazy to check the statement «the relation \( x \) to \( \pi(x) \) upon transition from this degree of ten to the subsequent all the time increases approximately on 2,3» [14] and results of calculations provided in table 5.

<table>
<thead>
<tr>
<th>Digit ( t_n )</th>
<th>Several PN1 Gauss [14]</th>
<th>Complete series PN2 [5]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( x / \pi(x) ) multiplicity</td>
<td>( x / \pi(x) ) multiplicity</td>
</tr>
<tr>
<td>1</td>
<td>2.5</td>
<td>1.6667</td>
</tr>
<tr>
<td>2</td>
<td>4.0</td>
<td>1.60</td>
</tr>
<tr>
<td>3</td>
<td>6.0</td>
<td>1.50</td>
</tr>
<tr>
<td>4</td>
<td>8.1</td>
<td>1.35</td>
</tr>
<tr>
<td>5</td>
<td>10.4</td>
<td>1.28</td>
</tr>
<tr>
<td>6</td>
<td>12.7</td>
<td>1.22</td>
</tr>
<tr>
<td>7</td>
<td>15.0</td>
<td>1.18</td>
</tr>
<tr>
<td>8</td>
<td>17.4</td>
<td>1.16</td>
</tr>
<tr>
<td>9</td>
<td>19.7</td>
<td>1.13</td>
</tr>
<tr>
<td>10</td>
<td>22.0</td>
<td>1.12</td>
</tr>
</tbody>
</table>

Here number 2,30 even among Gauss isn't present (if is, the error of approach to 2,30 even at four (actually their six) prime numbers is equal in ten 100(2,5 – 2,3) / 2,3 = 8,70%, that is a lot of). But, really, there is an aspiration of frequency rate to 1.

The complete series of prime numbers thus offered by us gives at the beginning of an interval of categories closer to Ig10 frequency rate 2,22 (the mistake makes 3,47% that is also significant in the statistical analysis). Equipotent both
sets of \( \text{PN}_1 \) and \( \text{PN}_2 \) can be accepted, only starting with categories \( i_{10} \geq 9 \) in a decimal numeral system.

Gauss's statement only about convergence of frequency rate of two adjacent categories \( i_{10} \) with growth \( x \) to 1 is true. For the proof of it we identify the death law according to table 5.

For a complete series of positive prime numbers the formula was received

\[
\text{card}(x_i / \pi(x_i)/(x_{i-1}/\pi(x_{i-1}))) = 1.09980 + 1788.3966 \exp(-6,20754_{10}^{0.20896}) .
\]  

The equation (20) shows that cardinal numbers as the relations of the subsequent value of relative power of prime numbers to the previous value, won't come nearer to unit, and can reach on a formula (20) only value 1.09980. From article [14] we read further: «Having carried out more careful and full calculations, Legendre in 1808 found out that especially good approach turns out if to subtract from \( \ln x \) not 1, but 1.08366, i.e. \( \pi(x) \sim \frac{x}{\ln x - 1.08366} \).»

In our formula (20), the constant 1.09980 little different from the number of Legendre 1.08366.

**XXV. APPROXIMATION ERROR**

So, a number of positive prime numbers on relative power was studied with the translation of prime numbers from a decimal numeral system in a numeral system with the basis \( e = 2,718281828 \ldots \) natural logarithms. It is known that this system possesses the greatest density of a data recording and treats nonintegral position numeral systems.

But non-integral numbers don't belong to natural numbers and the more so don't belong to traditional for Gauss's times to a number of prime numbers \([2,3,5,7,11,13,17,\ldots] \).

Thus, transformation appeared \( \ln 10 = 2.302585 \ldots \) the strong posteriorization leading to false identification of physical and mathematical regularities at different types of ranks of prime numbers, including here and so-called special ranks [5].

From Gauss's «easy» hand in mathematics the idealized theory of approximation which allowed to linearized easily a scale of abscissa scale through logarithms \( \ln x \) roughly developed. Thereby there is a radical restructuring of the statistical data presented in the beginning in a decimal numeral system, in a logarithmic scale. As a result the regularities closed on a design different from open mathematical constructs from table 3 are formed. Closed on substantial sense (in logarithms) not only it is difficult to understand empirical formulas, but they lose also presentation graphic (and the more so, physical) representations. Therefore mathematicians fondly counts up to these that series of prime numbers have no geometrical ideas.

As a result of Gauss, because of trembling love to the table of logarithms at 15-year age, he led the theory of numbers and then all mathematicians of the theory of statistics to the world of natural logarithms.

It is necessary the theory of approximation linear (special cases) and linearized through a natural logarithm (withdrawal to the world of logarithmic changed coordinates) the equations to cover with the theory of identification by nonlinear laws from table 3. Thus the well-known law of Gauss on normal distribution becomes only an idealized special case from the overall design (18).

**XXVI. CONCLUSION**

The well-known physicist Stephen Hoking supports idea of leaving from a mathematical formalism. The exit after all is, and it besides follows from work of Bristol group. Their analysis shows that the quantity of the mathematical formulas placed in appendices to biological articles, doesn't influence in any way their quoting. Hence their recipe - less formulas in the main body of the article, but more explain text, allowing the reader to understand the basic ideas of the theory and its applications [3].

And we arrived, having provided in article a large number of illustrations and detailed explanations.

At information and technological level Gilbert's 23rd problem (development of methods of calculus of variations) was solved by us long ago. Us, students and graduate students were modeled to hundred thousand examples from different areas of science and equipment.

Therefore the variation of functions is reduced to conscious selection of steady laws and designing on their basis of adequate steady regularities. But the technology of identification still completely wasn't published. The matter is that each example of tabular model has the specifics. So and software environment is not adapted to the process of identifying the generalized formula (18).

To attract the attention of the scientific community, had to tighten the selection of examples for statistical modeling. It turned out that the technological and socio-economic statistical data have a very large error, and biological tabular data is not enough. It is difficult to persuade biologists to wave oscillatory perturbations of natural objects. So we gradually came to the 8-th Hilbert problem and decided famous Riemann hypothesis about the root of \( 1/2 \) [5, 8].

Published nearly two years ago, the book [5] yet didn't receive a sufficient response, maybe, because it is written in Russian.

Therefore we decided to change radically and a number of prime numbers, having made it symmetric or asymmetric concerning a scale of integers \(-\infty < z < +\infty \). Critical points of an asymmetric traditional Gaussian series of the prime numbers located on an axis of natural numbers, were in the center of symmetry of a series of the whole prime numbers.

Thus the fundamental law of distribution of WPN was so simple on proportionality coefficient that much increased adequacy of statistical regularities. To compare to formulas of power of quantity of the prime numbers which are in decimal categories, became even inconvenient: known formulas of distribution of prime numbers in categories of a decimal numeral system are so rough on an error.

Perhaps now mathematicians, physicists, biologists and others will pay attention to this article?

The answer to the question of why mathematics is not engaged directly by the distribution of prime numbers, and carried away the centuries of the largest prime number identification and study of relative abundance (power set) of prime numbers among the natural numbers, convincingly explained Don Zagier [14].

Rejection by mathematicians 0 and 1 ahead of a traditional series \( a(n) = [2,3,5,\ldots] \) of prime numbers made a powerful
psychological barrier. Besides it is very strongly stirred to the
Gaussian order \( n = \{1,2,3,4,5,6,\ldots\} \) of a prime number
beginning only with unit. Sorting Euclid's [14] proof, became
clear that timely recognition of zero by Europeans and,
respectively, achievements of mathematics from Indians,
would allow, on a last and large measure, to reduce creation of
the new theory of prime numbers by two thousand years. After
all in Ancient Egypt already knew about binary notation.
About it was well shown in a cycle of films on the history of
mathematics.

Mathematicians made two large oversights:
1) didn't recognize 0, and some and 1, for prime numbers
and didn't understand that the beginning 0, 1, 2 and 3 at a
complete series of prime numbers undertakes from a series of
natural numbers;
2) in formulas of decomposition didn't understand binary
notation.

A traditional series of prime numbers is artificially
complicated by refusal of inclusion of elements 0 and 1 of a
series of natural numbers. Tendencies of centuries-old
non-recognition in Europe of zero for natural number were
very strong. In a series of natural numbers 0, 1, 2, 3, 4, 5, 6, 7,
8, 9 there are six prime numbers, three of which (0, 1, 2)
critical, and three more numbers (3, 5, 7) - noncritical.

In the zero block of the whole prime numbers there is
"wall" of dzeta-function of Riemann, it is geometrically
evident, and this wall grows with increase of number of
couples of whole prime numbers.

The maximum absolute error of relative power (the number
of prime numbers in decimal digits) a traditional Gaussian
row more than three times is higher than quantity of prime
numbers in comparison with a complete series of [5, 7] prime
numbers and is 30 times more rough in comparison with a
number of the whole prime numbers.

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